

## Continuum Modeling With Emphasis on Geotechnical

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UC Berkeley

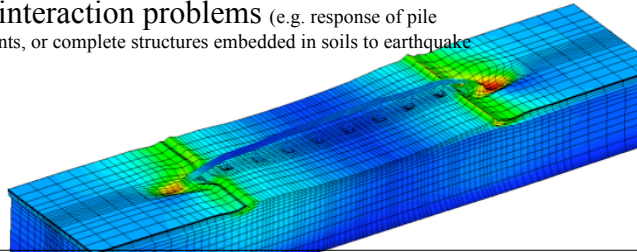
OpenSees Days Shanghai 2011



## Outline of Presentation

- Why
- Elements for Continuum Modeling
- Materials for Continuum Modeling
- Simple Examples

- Static Problems
  - Deformation analyses
  - Consolidation problems (diffusion problems)
  - Soil-structure interaction problems
    - Shallow foundations (e.g. bearing capacity, settlements)
    - Pile foundations (e.g. vertical and lateral capacity)
  
- Dynamic (earthquake problems)
  - Free-field analysis
  - Liquefaction induced problems
  - Soil structure interaction problems (e.g. response of pile foundations, bridge bents, or complete structures embedded in soils to earthquake excitations)



## Single & Multiphase Models

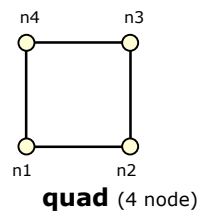
- Single Phase Models
  - Structural Modeling
  - Dry Soils
  
- Multi Phase Models
  - Phase 1 for Soil Skeleton
  - Phase 2 for Water (Pore Pressure)

## nD Materials

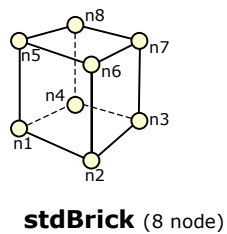
- Materials:
  - Elastic
  - DruckerPrager
  - J2 (VonMises)
  - Cam-Clay
  - PressureDependMultiYield (sand)
  - PressureIndependMultiYield (clay)
  - others

## Single Phase Elements

- Quad (4,9 nodes)

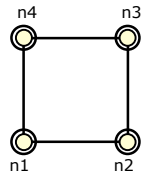


- Brick (8, 20 nodes)

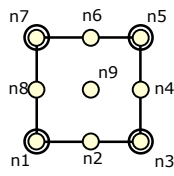


# Multi Phase Elements

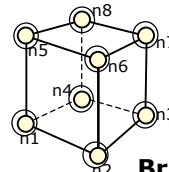
- Fully coupled u-p elements (2D & 3D)
- Fully coupled u-p-U elements (3D) for small deformations



**quadUP**



**9\_4\_quadUP**



**BrickUP**

Degrees of Freedom (DOFs) are:

- u → solid displacement, on
- P → pore fluid pressures, on
- U → pore fluid displacements, on

# Simply Supported Beam

n.tcl

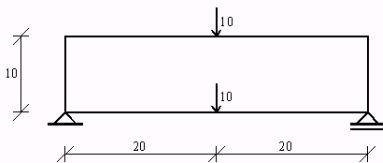


Fig. 1 Geometry and static loads

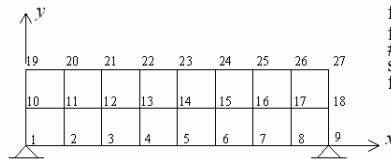


Fig. 2 Finite element mesh and node numbering

```

# some problem parameters
set L 40.0
set H 10.0
set thick 2.0
set P 10
set nX 9; # numNodes x dirn
set nY 3; # numNodes y dirn
# model builder
model Basic -ndm 2 -ndf 2
# create material
nDMaterial ElasticIsotropic 1 1000 0.25 3.0
# create nodes
set nodeTag 1
set yLoc 0.0;
for {set i 0} {$i < $nY} {incr i 1} {
  set xLoc 0.0;
  for {set j 0} {$j < $nX} {incr j 1} {
    node $nodeTag $xLoc $yLoc
    set xLoc [expr $xLoc+ $L/($nX-1.0)]
    incr nodeTag
  }
  set yLoc [expr $yLoc+ $H/($nY-1.0)]
}
# boundary conditions
fix 1 1 1
fix $nX 1 1
# create elements
set eleTag 1
for {set i 1} {$i < $nY} {incr i 1} {
  set iNode [expr 1+($i-1)*$nX];
  set jNode [expr $iNode+1];
  set kNode [expr $jNode+$nX];
  set lNode [expr $iNode+$nX];
  for {set j 1} {$j < $nX} {incr j 1} {
    element quad $eleTag $iNode $jNode $kNode $lNode
    $thick "PlaneStress" 1
    incr eleTag; incr iNode; incr jNode; incr kNode; incr lNode
  }
}
# apply loads
set midNode [expr ($nX+1)/2]
timeSeries Linear 1
pattern Plain 1 1 {
  load $midNode 0 -$P
  load [expr $midNode+ $nX*($nY-1)] 0 -$P
}
analysis Static;
analyze 1; print node $midNode

```

# Simply Supported Beam

o.tcl

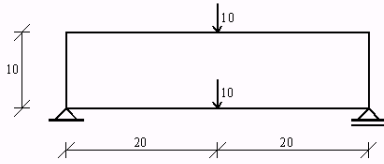


Fig. 1 Geometry and static loads

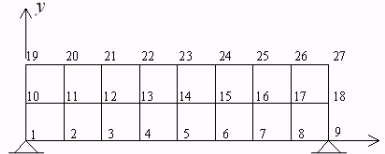


Fig. 2 Finite element mesh and node numbering

```
# some problem parameters
set L 40.0
set H 10.0
set thick 2.0
set P 10
set nX 9; # numNodes x dim
set nY 3; # numNodes y dim
```

```
# model builder
model Basic -ndm 2 -ndf 2
# create material
nDMaterial ElasticIsotropic 1 1000 0.25 3.0
```

```
# use block command
set cmd "block2D [expr $nX-1] [expr $nY-1] 1 1 \
quad \ " $thick PlaneStress 1" {
1 0 0
2 $L 0
3 $L $H
4 0 $H
}"
```

## eval Scmd

```
# apply loads
set midNode [expr ($nX+1)/2]
timeSeries Linear 1
pattern Plain 1 1 {
load $midNode 0 -$P
load [expr $midNode + $nX*($nY-1)] 0 -$P
}
analysis Static;
analyze 1;
print node $midNode
```

```
Terminal — bash — 85x37
examples> OpenSees n.tcl

OpenSees -- Open System For Earthquake Engineering Simulation
Pacific Earthquake Engineering Research Center -- 2.3.0.alpha

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Node: 5
Coordinates : 20 0
Disps: -1.37853e-16 -0.096041
unbalanced Load: 0 -10
ID : 26 27

examples> OpenSees o.tcl

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Node: 5
Coordinates : 20 0
Disps: -1.37853e-16 -0.096041
unbalanced Load: 0 -10
ID : 26 27

examples> 
```



## Lateral Pile Analysis

```

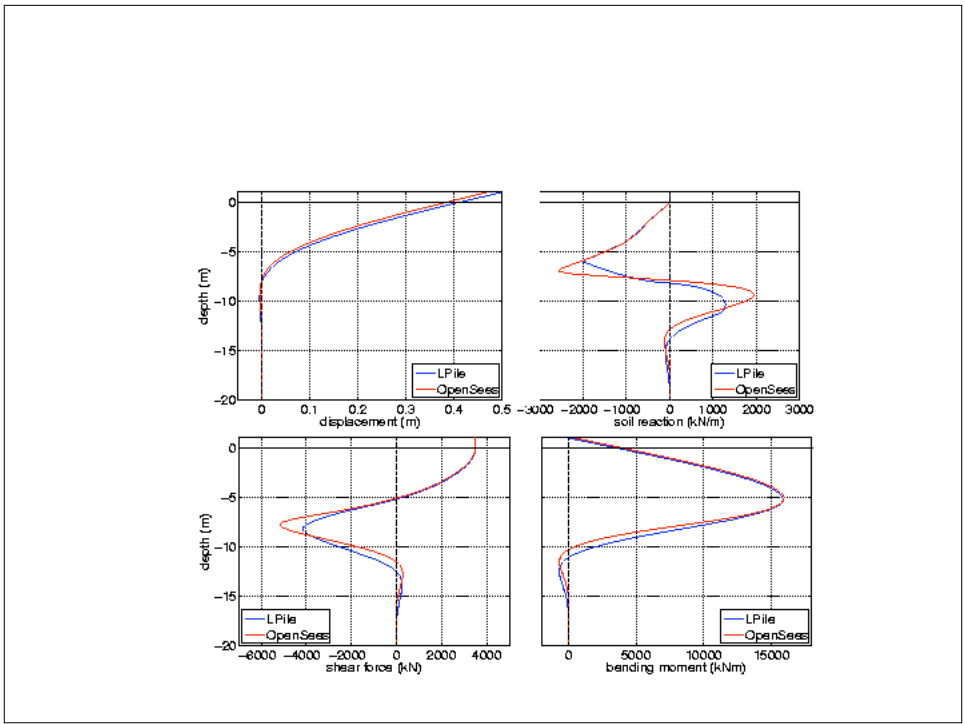
set L1 1.0; # length of pile head (above ground surface) (m)
set L2 2.0; # length of embedded pile (below ground surface) (m)
set diameter 1.0; # pile diameter
set nNodePile $N; # number of pile elements
set eleSize [expr ($L1+$L2)/$nNodePile]; # pile elem
# number of total pile nodes
set nNodeElem [expr 1 + $nNodePile]
# spring nodes created with 3 dim, 3 dof
model Basic -ndm 3 -ndf
# counter to determine number of embedded nodes
set count 0
# create spring nodes
for {set i 1} {$i <= $nNodePile} {incr i} {
  set zCoord [expr $eleSize*(i-1)]
  # only create spring nodes over embedded length o
  if {$zCoord <= $L2} {
    node $i 0.00 0.00 $zCoord
    node [expr $i+100] 0.00 0.00 $zCoord
    set count [expr $count+1]
  }
}
# number of embedded nodes
set nNodeEmbed $count
# spring node fixities
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  fix $i 1 1 1
  fix [expr $i+100] 0 1 1
}
# soil properties
set gamma 17.0; # soil unit weight (kN/m^3)
set phi 36.0; # soil internal friction angle (degrees)
set Gsoil 15000; # soil shear modulus at pile tip (k)
set puSwitch 1; # select pult definition method for i
set kSwitch 1; # variation in coefficient of subgrade i
# create spring material objects
source get_pyParam.tcl
source get_tzParam.tcl
source get_qzParam.tcl
# p-y spring material
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  # depth of current py node
  set pyDepth [expr $L2 - $eleSize*(i-1)]
  set pyParam [get_pyParam $pyDepth $gamma $phi]
  set pult [index $pyParam 0]
  set y50 [index $pyParam 1]
  uniaxialMaterial PySimple1 $i 2 $pult $y50 0.0
}
# t-z spring material
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  # depth of current tz node
  set tzDepth [expr $eleSize*(i-1)]
  # vertical effective stress at current depth
  set sigV [expr $gamma*$tzDepth]
  set tzParam [get_tzParam $sigV $diameter $sigV $eleSize]
  set tult [index $tzParam 0]
  set z50 [index $tzParam 1]
  uniaxialMaterial TzSimple1 [expr $i+100] 2 $tult $z50 0.0
}
# q-z spring material
# vertical effective stress at pile tip, no water table (depth is embedded pile length)
set sigVq [expr $gamma*$L2]
set qzParam [get_qzParam $sigVq $diameter $sigVq $Gsoil]
set qult [index $qzParam 0]
set z50q [index $qzParam 1]
uniaxialMaterial QzSimple1 101 2 $qult $z50q 0.0 0

```

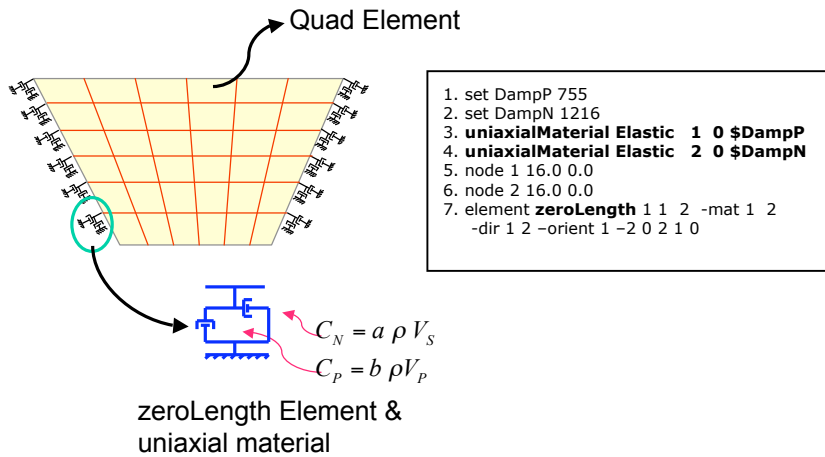
```

# element at the pile tip (has q-z spring)
element zeroLength 1001 1 101 -mat 1 101 -dir 1 3
# remaining elements
for {set i 2} {$i <= $nNodeEmbed} {incr i} {
  element zeroLength [expr $i+1000] $i [expr $i+100] -mat $i [expr $i+100]
}
puts "Finished creating all zero-Length elements for springs..."
# pile nodes created with 3 dimensions, 6 degrees of freedom
model BasicBuilder -ndm 3 -ndf 6
# create pile nodes
for {set i 1} {$i <= $nNodePile} {incr i} {
  # z-coordinates of nodes depend on element length
  set zCoord [expr $eleSize*(i-1)]
  node [expr $i+200] 0.00 0.00 $zCoord
}
puts "Finished creating all pile nodes..."
# create coordinate-transformation object
geom Transf Linear 1 0.0 -1.0 0.0
# create fixity at pile head (location of loading)
fix [expr 200+$nNodePile] 0 1 0 1 0 1
# create fixities for remaining pile nodes
for {set i 201} {$i <= [expr 200+$nNodePile]} {incr i} {
  fix $i 0 1 0 1 0 1
}
puts "Finished creating all pile node fixities..."
# define equal dof between pile and spring nodes
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  equalDOF [expr $i+200] [expr $i+100] 1
}
# elastic pile section
source elasticPileSection.tcl
for {set i 201} {$i <= [expr 200+$nNodePile]} {incr i} {
  element dispBeamColumn $i $i [expr $i-1] $secTag3D 3 1
}
setTime 10.0
# apply point load at the uppermost pile node in the x-direction
pattern Plain 10 {Series -time {0 10 20 10000} -values {0 0 1 1} -factor 1} {
  load [expr 200+$nNodePile] 3500 0.0 0.0 0.0 0.0 0.0
}
# create the analysis
integrator LoadControl 0.05
numberer RCM
system SparseGeneral
constraints Transformation
test NormDispIncr 1e-5 20 1
algorithm Newton
analysis Static
analyze 201

```



# Absorbent Boundaries Lysmer (1969)



## Other useful **tcl** scripts @

- <http://opensees.berkeley.edu/>
- <http://sokocalo.engr.ucdavis.edu/~jeremic>
- <http://cyclic.ucsd.edu/opensees/>
- [http://www.ce.washington.edu/~geotech/opensees/P EER/davis\\_meeting/](http://www.ce.washington.edu/~geotech/opensees/P EER/davis_meeting/)