

## Continuum Modeling With Emphasis on Geotechnical

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UC Berkeley

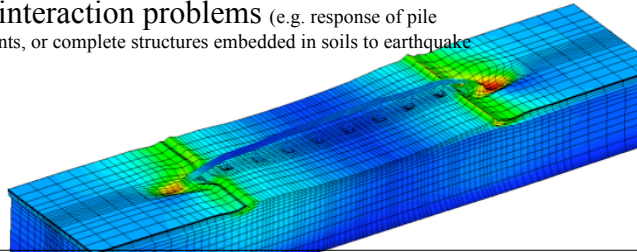
OpenSees Days Shanghai 2011



## Outline of Presentation

- Why
- Elements for Continuum Modeling
- Materials for Continuum Modeling
- Simple Examples

- Static Problems
  - Deformation analyses
  - Consolidation problems (diffusion problems)
  - Soil-structure interaction problems
    - Shallow foundations (e.g. bearing capacity, settlements)
    - Pile foundations (e.g. vertical and lateral capacity)
  
- Dynamic (earthquake problems)
  - Free-field analysis
  - Liquefaction induced problems
  - Soil structure interaction problems (e.g. response of pile foundations, bridge bents, or complete structures embedded in soils to earthquake excitations)



## Single & Multiphase Models

- Single Phase Models
  - Structural Modeling
  - Dry Soils
  
- Multi Phase Models (Soil + Water)
  - Phase 1 for Soil Skeleton
  - Phase 2 for Water (Pore Pressure)

## nD Materials

- Materials:
  - Elastic
  - DruckerPrager
  - J2 (VonMises)
  - Cam-Clay
  - PressureDependMultiYield (sand)
  - PressureIndependMultiYield (clay)
  - others

## Additional commands for **multiyield** materials

- Help perform stage analysis

```
updateMaterialStage -material $matTag -stage $sNum
```

\$MatTag → the tag of previously defined material

\$sNum → (0 - elastic, 1-plastic, 2 - linear elastic constant  $f(\sigma_3)$  )

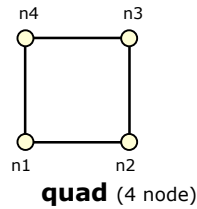
```
updateParameter -material $matTag -refG $newVal
```

\$MatTag → the tag of previously defined material

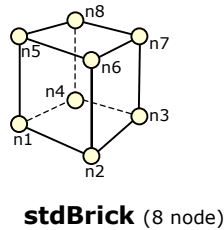
\$sNewVal → new parameter value

## Single Phase Elements

- Quad (4,9 nodes)

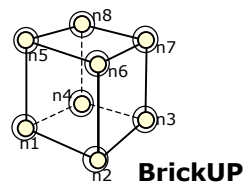
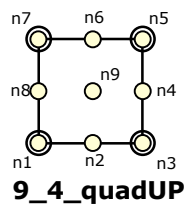
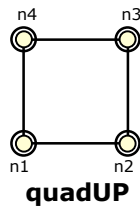


- Brick (8, 20 nodes)






## Multi Phase Elements

- Fully coupled u-p elements (2D & 3D)
- Fully coupled u-p-U elements (3D) for small deformations



Degrees of Freedom (DOFs) are:

- u → solid displacement, on 
- P → pore fluid pressures, on 
- U → pore fluid displacements, on 

# Simply Supported Beam

n.tcl

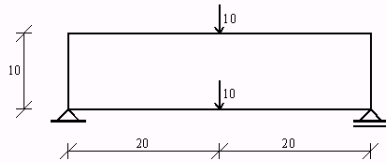


Fig. 1 Geometry and static loads

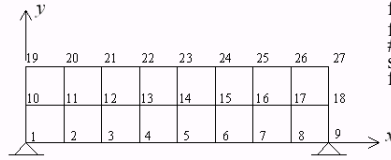


Fig. 2 Finite element mesh and node numbering

```
# some problem parameters
set L 40.0
set H 10.0
set thick 2.0
set P 10
set nX 9; # numNodes x dirn
set nY 3; # numNodes y dirn

# model builder
model Basic -ndm 2 -ndf 2

# create material
nDMaterial ElasticIsotropic 1 1000 0.25 3.0
```

```
# create nodes
set nodeTag 1
set yLoc 0.0;
for {set i 0} {$i < $nY} {incr i 1} {
  set xLoc 0.0;
  for {set j 0} {$j < $nX} {incr j 1} {
    node $nodeTag $xLoc $yLoc
    set xLoc [expr $xLoc+ $L/($nX-1.0)]
    incr nodeTag
  }
  set yLoc [expr $yLoc+ $H/($nY-1.0)]
}

# boundary conditions
fix 1 1 1
fix $nX 1 1

# create elements
set eleTag 1
for {set i 1} {$i < $nY} {incr i 1} {
  set iNode [expr 1+(Si-1)*$nX];
  set jNode [expr $iNode+1];
  set kNode [expr $jNode+$nX]
  set lNode [expr $iNode+$nX]
  for {set j 1} {$j < $nX} {incr j 1} {
    element quad $eleTag $iNode $jNode $kNode $lNode
    $thick "PlaneStress" 1
    incr eleTag; incr iNode; incr jNode; incr kNode; incr lNode
  }
}

# apply loads
set midNode [expr ($nX+1)/2]
timeSeries Linear 1
pattern Plain 1 1 {
  load $midNode 0 -$P
  load [expr $midNode + $nX*(nY-1)] 0 -$P
}

analysis Static;
analyze 1; print node $midNode
```

# Simply Supported Beam

o.tcl

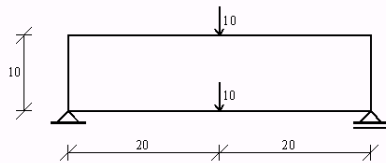


Fig. 1 Geometry and static loads

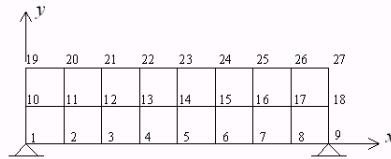


Fig. 2 Finite element mesh and node numbering

```
# some problem parameters
set L 40.0
set H 10.0
set thick 2.0
set P 10
set nX 9; # numNodes x dirn
set nY 3; # numNodes y dirn

# model builder
model Basic -ndm 2 -ndf 2

# create material
nDMaterial ElasticIsotropic 1 1000 0.25 3.0
```

```
# use block command
set cmd "block2D [expr $nX-1] [expr $nY-1] 1 1 \
  quad \ " $thick PlaneStress 1" {
  1 0 0
  2 $L 0
  3 $L $H
  4 0 $H
}"

eval $cmd

# apply loads
set midNode [expr ($nX+1)/2]
timeSeries Linear 1
pattern Plain 1 1 {
  load $midNode 0 -$P
  load [expr $midNode + $nX*(nY-1)] 0 -$P
}

analysis Static;
analyze 1;
print node $midNode
```

```

Terminal -- bash -- 85x37
examples> OpenSees n.tcl

OpenSees -- Open System For Earthquake Engineering Simulation
Pacific Earthquake Engineering Research Center -- 2.3.0.alpha

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(Copyright and Disclaimer @ http://www.berkeley.edu/OpenSees/copyright.html)

Node: 5
Coordinates : 20 0
Disps: -1.37853e-16 -0.096041
unbalanced Load: 0 -10
ID : 26 27

examples> OpenSees o.tcl

OpenSees -- Open System For Earthquake Engineering Simulation
Pacific Earthquake Engineering Research Center -- 2.3.0.alpha

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All Rights Reserved
(Copyright and Disclaimer @ http://www.berkeley.edu/OpenSees/copyright.html)

Node: 5
Coordinates : 20 0
Disps: -1.37853e-16 -0.096041
unbalanced Load: 0 -10
ID : 26 27

examples> 

```

## Cantilevered Circular Column

p.tcl

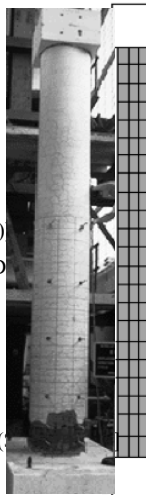
```

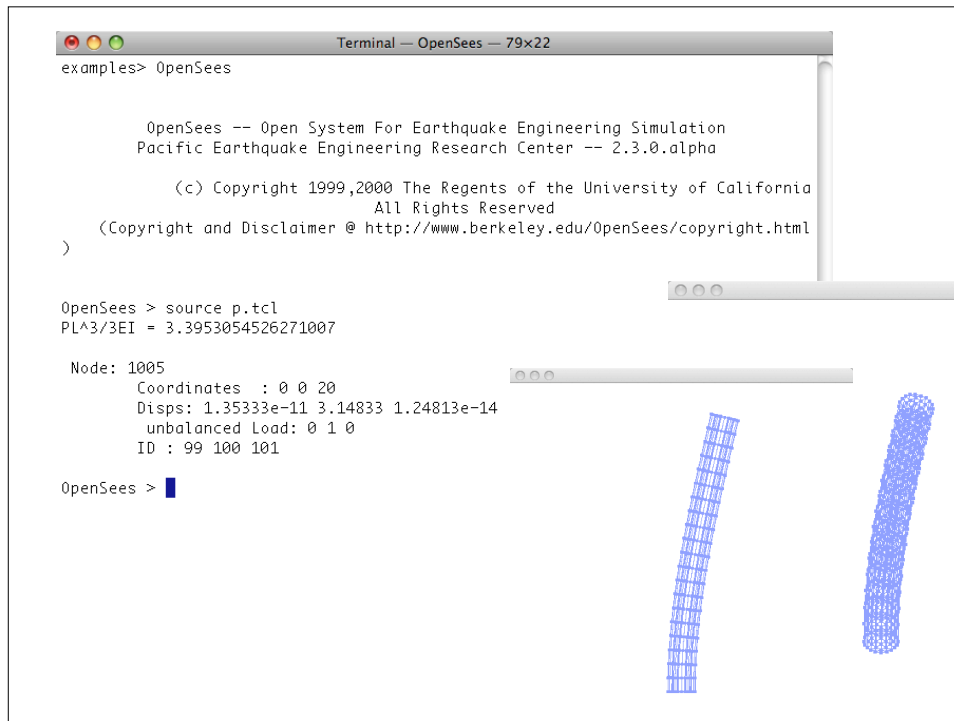
# mesh generation
set sqrtR [expr sqrt(SR/2.0)]
set cmd "block3D $nx $ny $nz 1 1 Sel
1 -$sqrtR -$sqrtR 0
2 $sqrtR -$sqrtR 0
3 $sqrtR $sqrtR 0
4 -$sqrtR $sqrtR 0
5 -$sqrtR -$sqrtR $L
6 $sqrtR -$sqrtR $L
7 $sqrtR $sqrtR $L
8 -$sqrtR $sqrtR $L
13 0 -$SR 0
14 SR 0 0
15 0 SR 0
16 -$SR 0 0
18 0 -$SR $L
19 SR 0 $L
20 0 SR $L
21 -$SR 0 $L
23 0 -$SR [expr $L/2.0]
24 SR 0 [expr $L/2.0]
25 0 SR [expr $L/2.0]
26 -$SR 0 [expr $L/2.0]
}"
eval $cmd

# boundary conditions
fixZ 0.0 1 1 1

# Constant point load
pattern Plain 1 Linear {
load $nn 0.0 $P 0.0
}

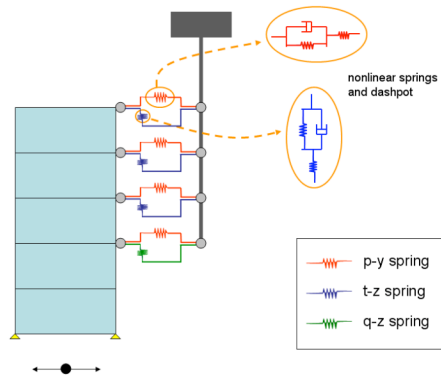
```





## Uniaxial models for Soil-Structure Interaction Models

- To capture interface response between solid (soil) and beam elements (pile)



Py Tz Qz Uniaxial Materials

- PySimple1
- TzSimple1
- QzSimple1
- PyLiq1
- TzLiq1

## Lateral Pile Analysis

```

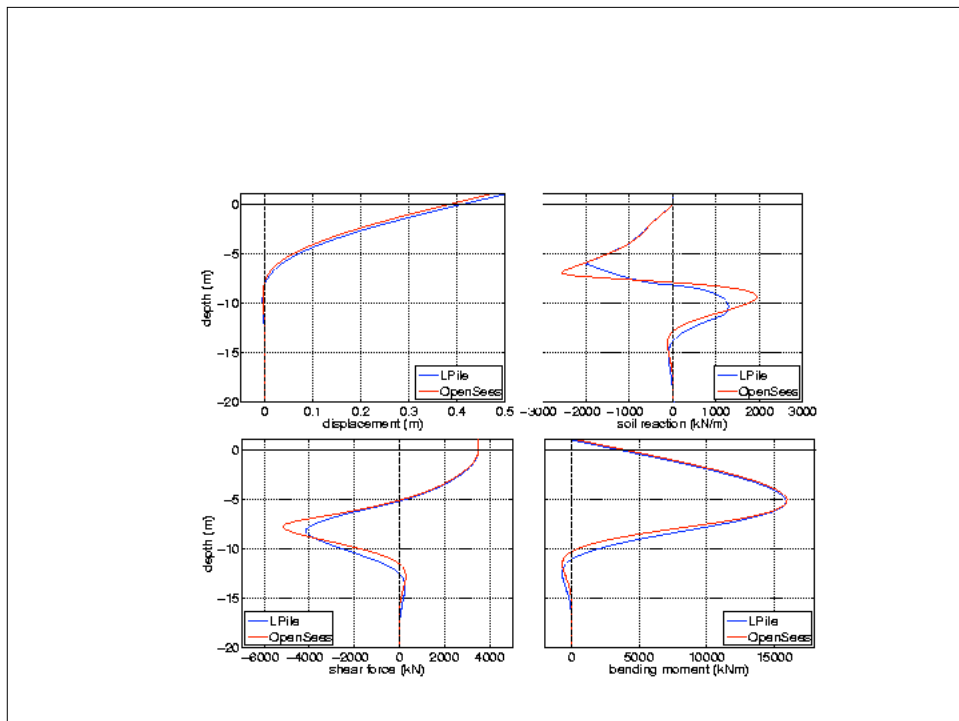
set L1 1.0; # length of pile head (above ground surface) (m)
set L2 2.0; # length of embedded pile (below ground surface) (m)
set diameter 1.0; # pile diameter
set nNodePile $N; # number of pile elements
set eleSize [expr ($L1+$L2)/$nNodePile]; # pile elem
# number of total pile nodes
set nNodeEmbed [expr 1 + $nNodePile]
# spring nodes created with 3 dim, 3 dof
model Basic -ndm 3 -ndf
# counter to determine number of embedded nodes
set count 0
# create spring nodes
for {set i 1} {$i <= $nNodePile} {incr i} {
  set zCoord [expr $eleSize*(i-1)]
  # only create spring nodes over embedded length o
  if {$zCoord <= $L2} {
    node $i 0.00 0.00 $zCoord
    node [expr $i+100] 0.00 0.00 $zCoord
    set count [expr $count+1]
  }
}
# number of embedded nodes
set nNodeEmbed $count
# spring node fixities
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  fix $i 1 1 1
  fix [expr $i+100] 0 1 1
}
# soil properties
set gamma 17.0; # soil unit weight (kN/m^3)
set phi 36.0; # soil internal friction angle (degrees)
set Gsoil 15000; # soil shear modulus at pile tip (k)
set puSwitch 1; # select pult definition method for
set kSwitch 1; # variation in coefficient of subgrade
# create spring material objects
source get_pyParam.tcl
source get_tzParam.tcl
source get_qzParam.tcl
# p-y spring material
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  # depth of current py node
  set pyDepth [expr $L2 - $eleSize*(i-1)]
  set pyParam [get_pyParam $pyDepth $gamma $phi]
  set pult [index $pyParam 0]
  set y50 [index $pyParam 1]
  uniaxialMaterial PySimple1 $i 2 $pult $y50 0.0
}
# t-z spring material
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  # depth of current tz node
  set tzDepth [expr $eleSize*(i-1)]
  # vertical effective stress at current depth
  set sigV [expr $gamma*$tzDepth]
  set tzParam [get_tzParam $sigV $diameter $sigV $eleSize]
  set tult [index $tzParam 0]
  set z50 [index $tzParam 1]
  uniaxialMaterial TzSimple1 [expr $i+100] 2 $tult $z50 0.0
}
# q-z spring material
# vertical effective stress at pile tip, no water table (depth is embedded pile length)
set sigVq [expr $gamma*$L2]
set qzParam [get_qzParam $sigVq $diameter $sigVq $Gsoil]
set qult [index $qzParam 0]
set z50q [index $qzParam 1]
uniaxialMaterial QzSimple1 101 2 $qult $z50q 0.0 0

```

```

# element at the pile tip (has q-z spring)
element zeroLength 1001 1 101 -mat 1 101 -dir 1 3
# remaining elements
for {set i 2} {$i <= $nNodeEmbed} {incr i} {
  element zeroLength [expr $i+1000] $i [expr $i+100] -mat $i [expr $i+100] -dir 1 3
}
puts "Finished creating all zero-Length elements for springs..."
# pile nodes created with 3 dimensions, 6 degrees of freedom
model BasicBuilder -ndm 3 -ndf 6
# create pile nodes
for {set i 1} {$i <= $nNodePile} {incr i} {
  # z-coordinates of nodes depend on element length
  set zCoord [expr $eleSize*(i-1)]
  node [expr $i+200] 0.00 0.00 $zCoord
}
puts "Finished creating all pile nodes..."
# create coordinate-transformation object
geom Transf Linear 1 0.0 -1.0 0.0
# create fixity at pile head (location of loading)
fix [expr 200+$nNodePile] 0 1 0 1 0 1
# create fixities for remaining pile nodes
for {set i 201} {$i <= [expr 200+$nNodePile]} {incr i} {
  fix $i 0 1 0 1 0 1
}
puts "Finished creating all pile node fixities..."
# define equal dof between pile and spring nodes
for {set i 1} {$i <= $nNodeEmbed} {incr i} {
  equalDOF [expr $i+200] [expr $i+100] 1
}
# elastic pile section
source elasticPileSection.tcl
for {set i 201} {$i <= [expr 200+$nNodePile]} {incr i} {
  element dispBeamColumn $i $i [expr $i-1] $secTag3D 3 1
}
setTime 10.0
# apply point load at the uppermost pile node in the x-direction
pattern Plain 10 {Series -time {0 10 20 10000} -values {0 0 1 1} -factor 1} {
  load [expr 200+$nNodePile] 3500 0.0 0.0 0.0 0.0 0.0
}
# create the analysis
integrator LoadControl 0.05
numberer RCM
system SparseGeneral
constraints Transformation
test NormDispIncr 1e-5 20 1
algorithm Newton
analysis Static
analyze 201

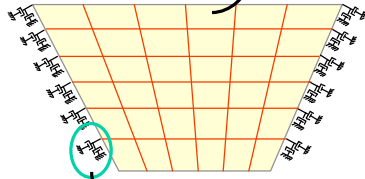
```





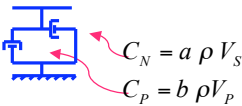
# Absorbent Boundaries Lysmer (1969)

Quad Element



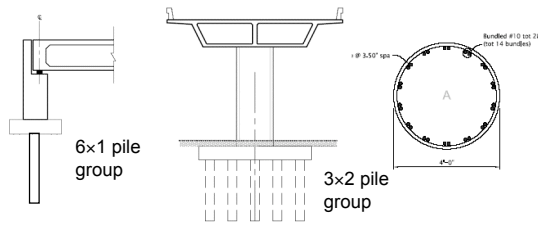
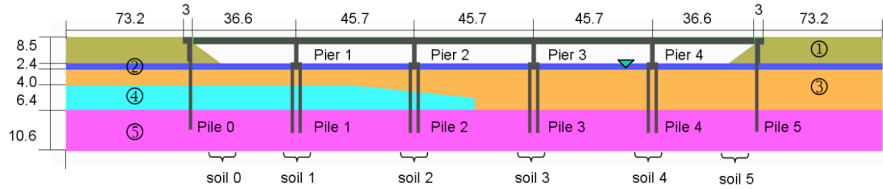
```

1. set DampP 755
2. set DampN 1216
3. uniaxialMaterial Elastic 1 0 $DampP
4. uniaxialMaterial Elastic 2 0 $DampN
5. node 1 16.0 0.0
6. node 2 16.0 0.0
7. element zeroLength 1 1 2 -mat 1 2
   -dir 1 2 -orient 1 -2 0 2 1 0
    
```



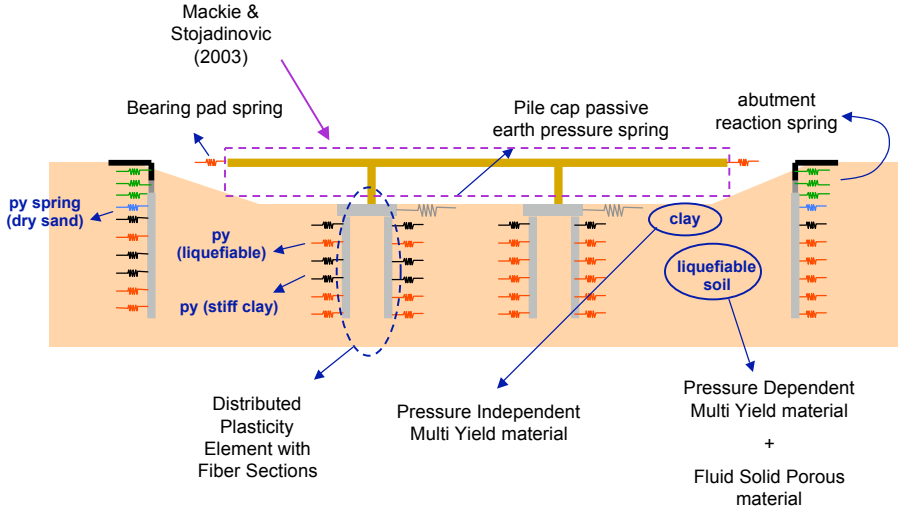
zeroLength Element &  
uniaxial material

## Target bridge system



- ① embankment
- ② med. stiff clay
- ③ loose-med sand
- ④ stiff clay
- ⑤ dense sand

# Numerical modeling for target bridge system



## Other useful **tcl** scripts @

- <http://opensees.berkeley.edu/>
- <http://sokocalo.engr.ucdavis.edu/~jeremic>
- <http://cyclic.ucsd.edu/opensees/>
- [http://www.ce.washington.edu/~geotech/opensees/PEER/davis\\_meeting/](http://www.ce.washington.edu/~geotech/opensees/PEER/davis_meeting/)